

## 17. Notation.

Symbols	Meaning, Reference	Dimension
A,B,C,P,Q,R,S	reagents	-
A	intermaterial area	m <sup>2</sup>
A	cross-flow area in eqs.(2.74)÷(2.79)	m <sup>2</sup>
A <sub>c</sub>	cross-flow area	m <sup>2</sup>
A <sub>i</sub>	dimensionless rate of deformation	-
a	volume ratio	-
a	radius of core stream (chap. 4.4)	m
a <sub>v</sub>	intermaterial area per unit volume	m <sup>-1</sup>
C	dimensionless concentration	-
C	dimensionless wave speed (chap. 4)	-
C <sub>i</sub>	dimensionless concentration of substance i	-
C <sub>E</sub>	energetic cost of mixing	J/m <sup>3</sup>
c	concentration	mol/m <sup>3</sup> , mol/dm <sup>3</sup>
c	wave speed (chap. 2.5 and 4)	m/s
c <sub>i</sub>	concentration of substance i	mol/m <sup>3</sup> , mol/dm <sup>3</sup>
c <sub>∞</sub> (x), c <sub>∞</sub> (r)	universal concentration profiles	mol/m <sup>3</sup>
c <sub>A0</sub>	solubility of monomer in eq.(2.16)	kg/m <sup>3</sup>
$\overline{c_{i0}} = c_{i0}/(1+a)$	average initial concentration	mol/m <sup>3</sup> , mol/dm <sup>3</sup>
c <sub>NaOH</sub>	limiting concentration of NaOH	mol/kg
$\overline{c_u}, \overline{c_l}$	mean concentration in upper and lower part of diffusion chamber	mol/kg
c <sub>v</sub>	specific heat	J/(K·kg)
D	molecular diffusivity	m <sup>2</sup> /s
D	vessel diameter (chap. 2.4 and 7)	m
D <sub>i</sub>	molecular diffusivity of substance i	m <sup>2</sup> /s
D <sub>T</sub>	thermal diffusivity	m <sup>2</sup> /s
D <sub>ii</sub>	diagonal element of deformation tensor	s <sup>-1</sup>
$\overline{\overline{D}}$	deformation tensor	s <sup>-1</sup>
Da	Damköhler number	-
$\overline{Da} = Da/(1+a)$	modified Damköhler number	-
d	impeller diameter	m

d	separation distance in eqs.(2.64)÷(2.65)	m
d	inlet diameter (chap. 10)	m
E	activation energy	J/mol
E	residence time distribution (chap. 2)	s <sup>-1</sup>
E <sub>ij</sub>	kinetic energy of particle	J
e	energy input on mixing	J
e <sub>m</sub>	minimum energy input on mixing	J
eff	energetic efficiency of mixing	-
eff <sub>v</sub>	efficiency of mixing	-
erf	error function $erf(x) = \frac{2}{\sqrt{\pi}} \cdot \int_0^x e^{-x^2} dx$	-
F <sub>i</sub>	stoichiometric ratio	-
f, f <sub>i</sub>	concentration fraction	-
f	oscillation frequency (chap. 6 and 8)	Hz
G	shear rate	s <sup>-1</sup>
g	vector correlation coefficient	-
H	liquid depth in vessel	m
He	Heat release parameter	-
h	distance between planes inducing shear flow	m
I <sub>S</sub> , I <sub>SR</sub> , I <sub>SE</sub>	intensities of segregation	-
I <sub>kl</sub>	concentration moment	m <sup>2</sup>
i	imaginary unit	-
J <sub>i</sub>	molar stream	mol/(s·m <sup>2</sup> )
k, k <sub>1</sub> , k <sub>2</sub>	second-order reaction rate constants	m <sup>3</sup> /(mol·s) dm <sup>3</sup> /(mol·s)
L	scale of segregation (chap. 2.1)	m
L	length of cylinders in eqs.(2.64)÷(2.65)	m
L	length of mixing units in eq.(2.79)	m
L	reactor scale (chap. 2.3)	m
L	characteristic length scale (chap. 3 and 5.2)	m
L	total length of diffusion chamber (chap. 6)	m
l	width of feeding stream	m
l <sub>m</sub>	mean separation distance	m
l <sub>ij</sub>	distance separating points i and j	m
l <sub>∞</sub>	limiting penetration distance	m

$M$	amount of shear	-
$M_i^j$	dimensionless gradient concentration moment	-
$m$	feed discretization	-
$m_p$	particle mass	kg
$N$	number of mixing units in static mixer	-
$N_i$	number of moles of reactant $i$	mol
$\hat{N}, \hat{n}$	direction versors	-
$\dot{N}_i$	total number of moles consumed per unit area at reaction plane (chap. 5.2)	mol/m <sup>2</sup>
$\dot{N}_i$	molar inlet stream of reagent $i$ (chap. 10)	mol/s
$n$	impeller revolution speed	rev/s, rev/min
$n$	azimuthal mode number (chap. 2.5)	-
$n_T$	turbine revolution speed	rev/min
$P$	power input	W
$P$	pressure in undisturbed flow (chap. 2.5 and 4)	Pa
$P_M$	minimum power input on mixing	W
$P_T$	power input on liquid transport	W
$Po$	power number	-
$Pr$	Prandtl number	-
$p$	pressure	Pa
$p'$	pressure perturbation (chap. 2.5 and 4)	Pa
$Q$	volumetric flow	m <sup>3</sup> /s
$Q_c$	circulation flow	m <sup>3</sup> /s
$Q_f$	feeding rate	m <sup>3</sup> /s, cm <sup>3</sup> /min
$Q_v$	product output	s <sup>-1</sup>
$q$	heat release	J/kg
$R$	universal gas constant	J/(mol · K)
$R$	mixing unit radius in eq.(2.79)	m
$R$	filament radius (chap. 3)	m
$R$	pipe radius (chap. 4)	m
$R_i$	reaction rate	mol/(s · m <sup>3</sup> ) mol/(s · dm <sup>3</sup> )
$R_1, R_2$	radiuses of annular gap (chap. 8.2)	m
$Re$	Reynolds number	-

$Re_G$	generalized Reynolds number	-
$Re_s$	Reynolds number for annular gap	-
$Re_w$	Reynolds number for core stream (chap. 4)	-
$\vec{r}$	separation vector	m
$r, \theta, z$	polar coordinates	m, radians, m
$r_1, r_2$	radiuses of on-line mixer inlets	m
$Sc, Sc_i$	Schmidt numbers	-
$s$	striation thickness	m
$s$	slab thickness (chap. 3, 5, 7 and 9)	m
$T$	temperature	K, deg
$T$	dimensionless time (chap. 3)	-
$t$	time	s
$t_c$	characteristic scaling time	s
$t_c$	circulation time	s
$t_D$	characteristic diffusion time	s
$t_{DF}$	characteristic mixing time	s
$t_{D1/2}$	mixing time in "rigid" fluid	s
$t_{E1/2}$	mixing time in elongational flow	s
$t_F$	characteristic deformation time	s
$t_f$	lifetime of limiting reactant	s
$t_{fd}$	feeding time	s, min
$t_m$	mixing time	s
$t_R$	characteristic reaction time	s
$t_{res}$	residence time	s
$t_{S1/2}$	mixing time in shear flow	s
$\hat{t}$	tangential versor	-
$U, W$	radial and axial velocities of unperturbed flow	m/s
$U_x$	dimensionless translation velocity	-
$u, w$	radial and axial velocities	m/s
$u', w'$	radial and axial velocity perturbations	m/s
$V$	volume	m <sup>3</sup> , dm <sup>3</sup>
$V_i$	volume of solution i	m <sup>3</sup> , dm <sup>3</sup>
$V_i$	velocity components of undisturbed flow (chap. 2.5)	m/s

$v$	velocity	m/s
$v_i$	linear velocity components	m/s
$v_i'$	velocity perturbations (chap. 2.5)	m/s
$v_n$	normal velocity component	m/s
$v_r, v_\theta, v_z$	cylindrical velocity components	m/s
$v_r', v_\theta', v_z'$	cylindrical velocity perturbations (chap. 2.5)	m/s
$v_x, v_y, v_z$	linear velocity components	m/s
$v_x', v_i'$	velocity components in Lagrangian frame	m/s
$v_{ij}$	particle velocity	m/s
$\vec{v}$	velocity vector	m/s
$w_p$	weight fraction of polymer	-
$X$	selectivity	-
$X, Y, Z$	dimensionless distances (chap. 3 and 5.2)	-
$X, Y, Z$	relative changes of distances in eq.(2.10)	-
$\vec{X}$	position of Lagrangian point	m
$x, y, z$	Cartesian coordinates	m
$x_i$	Cartesian coordinate	m
$x', x_i'$	Cartesian coordinates in Lagrangian frame	m
$x_R$	position of reaction plane	m
$x_{\lambda/2}$	half wave length of instability	m
$\vec{x}$	position vector	m
$Y_i$	conversion of reagent i	-
$Ze$	Zel'dovich number	-
$\alpha$	rate of stretch	s <sup>-1</sup>
$\alpha$	wave number (chap. 2.5 and 4)	m <sup>-1</sup>
$\alpha'$	rate of stretch in rotating frame	s <sup>-1</sup>
$\alpha_i$	rate of deformation in direction i	s <sup>-1</sup>
$\alpha_x, \alpha_y, \alpha_z$	direction angles (chap. 2)	radians
$\alpha_x, \alpha_y, \alpha_z$	deformation rates (chap. 5.2)	s <sup>-1</sup>
$\beta$	deflection angle	radians
$\Gamma$	dimensionless time	-
$\Delta_i$	dimensionless displacement of reactant profile	-
$\Delta N_i$	number of moles consumed in reaction	mol
$\Delta p_{\text{mixer}}$	pressure drop in static mixer	Pa

$\Delta p_{\text{tube}}$	pressure drop in empty tube	Pa
$\delta$	layer thickness (chap. 2 and 8)	m
$\delta$	delta function (chap. 3)	-
$\delta$	phase shift (chap. 6)	deg
$\delta, \delta_i$	penetration distance (chap. 5.1, 7 and 9)	m
$\delta_i$	dimensionless gradient width (chap. 5.2 and 8)	-
$\delta_1, \delta_2$	width of regions in eq.(2.3)	m
$\delta_{kl}$	Kronecker's symbol	-
$\varepsilon$	rate of energy dissipation per unit volume	kg/(m · s <sup>3</sup> )
$\zeta_x$	denotes microflow element	-
$\eta$	area stretch	-
$\eta$	global stoichiometric balance (chap. 10)	-
$\theta = t_D/t_F$	characteristic time ratio (chap. 5.1, 7 and 9)	-
$\theta_T$	dimensionless temperature	-
$\kappa$	conductivity	S/cm
$\lambda$	stretch ratio	-
$\lambda$	wavelength (chap. 4)	m
$\lambda$	constant in Neumann's solution (chap 5.2)	-
$\lambda_x$	scale of microflow element	m
$\mu$	dynamic viscosity	Pa·s
$\nu$	kinematic viscosity	m <sup>2</sup> /s
$\nu_i$	stoichiometric coefficient	-
$\xi$	dimensionless position	-
$\xi$	disturbance of liquid-liquid interface (chap. 4)	m
$\vec{\xi}$	position vector in Lagrangian frame	m
$\xi_i$	Cartesian coordinates in Lagrangian frame	m
$\xi_R$	dimensionless position of reaction plane	-
$\Pi_1$	modified power number	-
$\Pi_2$	modified mixing time number	-
$\rho$	density	kg/m <sup>3</sup> , g/cm <sup>3</sup>
$\sigma$	interfacial surface tension	N/m
$\vec{\sigma}$	normal stress	N/m <sup>2</sup>
$\tau$	warped time	-
$\tau$	shear stress in eq.(2.8)	N/m <sup>2</sup>

$\tau$	relaxation time (chap. 6)	s
$\tau_{1/2}$	warped time related to $t_{E1/2}$ , $t_{S1/2}$ and $t_{D1/2}$	-
$\phi$	volume fraction	-
$\phi$	component of Stoke's stream function (chap. 2.5 and 4)	m <sup>3</sup> /s
$\phi$	$\varepsilon/\bar{\varepsilon}$ (chap. 7 and 9)	-
$\vec{\chi}$	vector motion function	m
$\psi$	Stoke's stream function (chap. 2.5 and 4)	m <sup>3</sup> /s
$\psi$	dimensionless rate of growth of reaction zone (chap. 5.1)	-
$\psi$	lamina deflection angle (chap. 3)	radians
$\overline{\overline{\Omega}}$	rotation tensor	s <sup>-1</sup>

### More Important Subscripts

c	continuous phase
d	dispersed phase
f	final value
max	maximum value
o	initial value
out	refers to outlet stream (chap. 4)
1	refers to central stream (chap. 4 and 10)
2	refers to annular stream (chap. 4 and 10)

### More Important Superscripts

-	mean value
T	matrix transposition
$\infty$	denotes far field value

### Special Symbols

	absolute value
Im	imaginary part
< >	environment variable
$\langle \rangle_{\zeta_x}$	mean in microflow element
$\langle \rangle_A$	area average

$\langle\langle \rangle\rangle_A$	mean flow average - $\langle\langle f \rangle\rangle_A = \langle v_n \cdot f \rangle_A / \langle v_n \rangle_A$
$\langle \rangle_V$	volume average
$\langle \rangle_{exit}$	mean at exit

### Differential Operators

$$\nabla = \left[ \frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right] \quad \text{in Cartesian coordinates}$$

$$\nabla = \left[ \frac{1}{r} \cdot \frac{\partial}{\partial r} r, \frac{1}{r} \cdot \frac{\partial}{\partial \theta}, \frac{\partial}{\partial z} \right] \quad \text{in polar coordinates}$$

$$\text{Grad} \vec{v} = \frac{\partial v_j}{\partial x_i} \quad i, j = 1, 2, 3$$

$$\frac{d}{dt} = \frac{\partial}{\partial t} + \sum_{i=1}^3 v_i \cdot \frac{\partial}{\partial x_i}$$

